

# Diffusion and binding constants for acetylcholine derived from the falling phase of miniature endplate currents

(acetylcholine receptor/acetylcholine receptor kinetics/buffered diffusion/neuromuscular junction/saturated disk model)

BRUCE R. LAND<sup>†</sup>, WILLIAM V. HARRIS<sup>†</sup>, EDWIN E. SALPETER<sup>‡</sup>, AND MIRIAM M. SALPETER<sup>†</sup>

<sup>†</sup>Section of Neurobiology and Behavior, Division of Biology, and <sup>‡</sup>Department of Physics, Cornell University, Ithaca, NY 14853

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**ABSTRACT** In previous papers we studied the rising phase of a miniature endplate current (MEPC) to derive diffusion and forward rate constants controlling acetylcholine (AcCho) in the intact neuromuscular junction. The present study derives similar values (but with smaller error ranges) for these constants by including experimental results from the falling phase of the MEPC. We find diffusion to be  $4 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$ , slightly slower than free diffusion, forward binding to be  $3.3 \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$ , and the distance from an average release site to the nearest exit from the cleft to be  $1.6 \mu\text{m}$ . We also estimate the back reaction rates. From our values we can accurately describe the shape of MEPCs under different conditions of receptor and esterase concentration. Since we suggest that unbinding is slower than isomerization, we further predict that there should be several short “closing flickers” during the total open time for an AcCho-ligated receptor channel.

The vertebrate neuromuscular junction has a high concentration of acetylcholine receptors (AcChoR) and very rapid physiological response to single quantal packets of acetylcholine (AcCho). We have combined measurements from the time course of miniature endplate currents (MEPCs) and AcChoR site densities,  $\sigma$ , with modeling of a standard kinetic scheme. The MEPC rising phase was discussed in previous papers (1, 2); the falling phase is discussed in the present paper. This allows us to derive the rate constants of diffusion and binding of AcCho and isomerization of the AcCho-activated ionic channel.

Recently, cation translocation studies and single-channel recordings (e.g., see refs. 3–6) have provided many kinetic parameters that predict MEPCs and single-channel wave forms. [For earlier values, see review by Heidmann and Changeux (7).] In our approach we use the shape of the MEPC as a function of AcChoR concentration to derive forward binding rates as well as information on AcCho diffusion in the intact neuromuscular cleft. We thus complement the results obtained by chemical techniques and by single-channel recording. The derived parameters support our motivating assumptions of the “saturating disk model” used by Salpeter and colleagues (8–11) to explain the generation of the MEPC.

## METHODS

We recorded MEPCs by voltage clamp from the intercostal muscle of the lizard *Anolis carolinensis*, using experimental techniques as in the first two papers of this series (1, 2) with minor modifications.

Three groups were used: (i) control muscle (esterases and receptor concentration unaltered); (ii) receptors intact and esterases fully inactivated [with 1 mM diisopropyl fluorophosphate (iPr<sub>2</sub>P-F) for 1 hr]; (iii) receptors partially inactivated [with 40 nM  $\alpha$ -bungarotoxin (BTX) for 40 min] to

$\approx 0.36$  its normal value (papers 1 and 2) and esterases inactivated with iPr<sub>2</sub>P-F as in *ii*. The filtering conditions of the voltage clamp were modified from those used in papers 1 and 2 to improve the signal-to-noise ratio. Because the falling phase of MEPCs is slow relative to the rise time, the signals were low-pass-filtered at 1 kHz (two-pole Butterworth filter) and the digitizer sampling rate was reduced to 6.25 kHz. Even though the Nyquist frequency is only a factor of 3 above our filter cutoff, aliasing was judged to be less than 4% of peak current. All experiments were done at  $22 \pm 1^\circ\text{C}$  and  $-100 \text{ mV}$  holding potential. Fall time ( $t_f$ ) values were obtained from the experimental MEPC as  $1.23 \times$  the 90–40% fall time. The factor 1.23 is the conversion from 90–40% to  $e$ -folding time for a pure exponential.

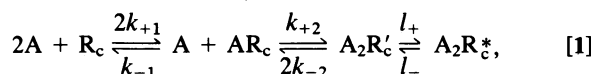
## RESULTS

Fig. 1 shows six examples of measured MEPC traces, illustrating the three conditions used in the present study. Fig. 2 plots the relation between  $t_f$  and MEPC amplitude  $A_c$ , and Table 1 gives the mean values of  $t_f$  and  $A_c$  under these conditions.

We confirm (12–15) that inactivation of esterases lengthens  $t_f$  appreciably and that, when  $\sigma$  is reduced by BTX treatment,  $t_f$  is somewhat shortened again (12, 15). Our additional observations are that, when esterases are intact,  $t_f$  does not depend on  $A_c$  (Fig. 2A), but after esterase inactivation  $t_f$  increases with increasing  $A_c$  (Fig. 2B). Finally, decreasing  $\sigma$ , with esterases inactivated, almost eliminates the correlation between  $t_f$  and  $A_c$  (Fig. 2C).

## Chemical Kinetics Scheme

We first assume that AcCho is released instantaneously from a very small area and diffuses in the cleft with diffusion constant  $D$ . A standard chemical kinetics scheme (16) is then assumed for the interaction of AcCho with receptor at any point in the cleft:



in which  $A$  is AcCho,  $A_2R'_c$  is the doubly bound AcChoR-channel complex in the closed conformation, and  $A_2R_c^*$  is that complex in the open conformation. In this scheme we

Definitions and abbreviations: AcCho, acetylcholine; AcChoR, acetylcholine receptor or single AcCho binding site;  $\sigma$ , AcChoR site density;  $R_c$ , AcChoR-channel complex—i.e., the unit consisting of the AcCho channel and the AcCho binding sites needed to activate it; iPr<sub>2</sub>P-F, diisopropyl fluorophosphate; BTX,  $\alpha$ -bungarotoxin; MEPC, miniature endplate current;  $A_c$ , MEPC amplitude;  $t_r$ , rise time;  $t_f$ ,  $1.23 \times$  90–40% fall time;  $N$ , number of AcCho molecules released per quantal packet;  $D$ , diffusion constant;  $R_{ex}$ , characteristic distance from release site to edge of receptor-containing cleft;  $g$ , fraction of doubly bound  $R_c$ s that are open;  $\chi_-$ , effective unbinding rate (see Eq. 2).

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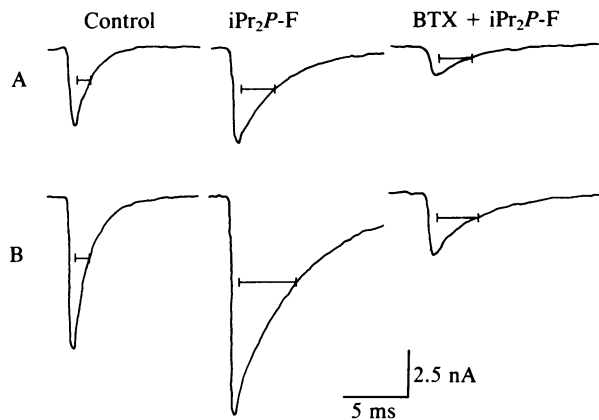


FIG. 1. Averaged MEPC traces of below (A) and above (B) mean amplitude for each of three experimental conditions (see *Methods*). Each trace is the average of some 100–400 individual MEPC recordings. The smaller traces (A) are  $\approx 0.7 \times$  mean  $A_c$  and the larger traces (B) are  $\approx 1.4 \times$  mean  $A_c$ . The bars extend from the 90% point to the 40% point in the falling phases. Note that  $iPr_2P$ -F-treated endplates produce longer and more amplitude-dependent MEPC fall times than either of the other two conditions (see also Fig. 2 and Table 1).

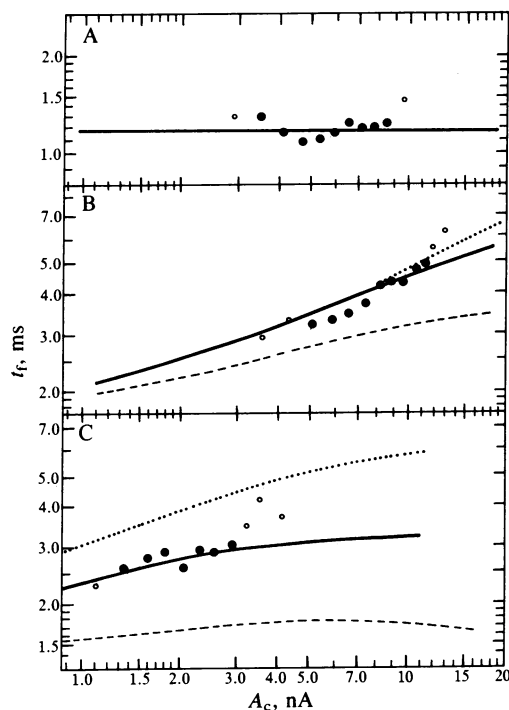


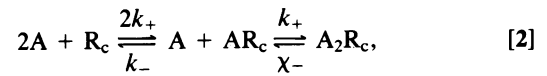
FIG. 2. Fall time vs. MEPC amplitude, showing both experimental points and model fits. Of the experimental points, ● represent amplitude bins used in the data analysis (having  $>100$  MEPCs), ○ represent amplitude bins with few traces ( $50 < n < 100$  MEPCs averaged). A shows that the MEPC fall times of control endplates (no  $iPr_2P$ -F or BTX) are independent of amplitude, whereas in B ( $iPr_2P$ -F-treated endplates) the  $t_f$ - $A_c$  correlation is strong and in C (BTX +  $iPr_2P$ -F-treated endplates) it is still positive but somewhat reduced. The model curves refer to quantities  $\chi_-$  and  $R_{ex}$  defined in the text. The horizontal (model) line in A corresponds to  $1/\chi_-$ . B compares data with three computed model curves with various distances  $R_{ex}$ : heavy curve for best value of  $R_{ex} = 1.6 \mu m$ , using Table 2 parameters; dotted curves for  $R_{ex} = 2.2 \mu m$ ; and broken curve for  $R_{ex} = 1.1 \mu m$  (all other model parameters kept constant). Note that the computed curves for  $R_{ex} \geq 1.6 \mu m$  are relatively close together, so that the model fit to  $iPr_2P$ -F data is relatively insensitive to large  $R_{ex}$ . C compares model curves with experimental data, as explained for B. It shows that when  $\sigma$  is reduced the fit is very sensitive to  $R_{ex}$ .

Table 1. Experimental results for amplitude  $A_c$  and fall time  $t_f$

Conditions	No. traces	$A_c$ , nA	$t_f$ , ms
Esterases intact	2224	$6.1 \pm 0.8$	$1.16 \pm 0.05$
$iPr_2P$ -F	3877	$7.9 \pm 1$	$4.0 \pm 0.2$
BTX + $iPr_2P$ -F	1003	$2.2 \pm 0.4$	$2.8 \pm 0.2$

The error ranges given are the statistical standard errors, plus an estimate for systematic measurement errors.

assume that there are two AcChoR binding sites per channel complex ( $R_c$ ), that both sites have to be occupied by AcCho to allow the opening of the channel, and that unbinding can occur only from the closed conformation. This scheme contains (in addition to the diffusion constant  $D$ ) six parameters: two binding constants ( $k_{+1}$  and  $k_{+2}$ ), two unbinding constants ( $k_{-1}$  and  $k_{-2}$ ), and two rate constants for a conformational change,  $l_+$  for channel opening and  $l_-$  for channel closing. (The  $k_+$  and  $k_-$  constants are for the individual binding sites of the two-site channel complex.) By varying  $\sigma$  experimentally (1, 2) we had subdivided the MEPC rise time,  $t_r$ , into a  $\sigma$ -dependent "reduced rise time" and a  $\sigma$ -independent time contribution that gives a lower limit to the relaxation rate for gating,  $(l_+ + l_-) \approx 25 \text{ ms}^{-1}$ . We assume throughout the present paper that there is no "direct cooperativity" in either the binding step or the unbinding step, so that  $k_{+1} = k_{+2} \equiv k_+$ ; and  $k_{-1} = k_{-2} \equiv k_-$  (we will discuss results for different assumed ratios of these values elsewhere). Because it is not easy to get a value for  $k_-$  independent of  $l_-$ , we shall use an abbreviated chemical kinetics scheme that omits the gating delay and combines isomerization constants with the unbinding constants  $2k_{-2}$ :



in which  $k_+ \equiv k_{+1} = k_{+2}$ ;  $A_2R_c = A_2R'_c + A_2R^*_c$  refers to any doubly bound complex (open or closed) and  $\chi_-$  is an effective unbinding rate. We define  $g = A_2R^*_c/A_2R_c$  as the fraction of doubly bound receptor complexes with an open channel. At isomerization equilibrium in Eq. 1, the ratio  $g/(1-g)$  of open to closed channels is  $l_+/l_-$  and  $g$  is  $l_+/(l_+ + l_-)$ . We shall argue for the assumption  $k_- < l_+ + l_-$ , in which case isomerization equilibrium is maintained during the falling phase. Because unbinding can occur only from the closed state, the effective unbinding rate  $\chi_-$  in Eq. 2 is related to the rate  $k_{-2}$  in Eq. 1 by

$$\chi_- = (1 - g)2k_{-2} = \frac{l_-}{l_+ + l_-} 2k_{-2}. \quad [3]$$

Thus, although we assume the absence of any "direct cooperativity" between  $k_{-1}$  and  $k_{-2}$ , we have the "apparent cooperativity" implied by  $\chi_- < 2k_-$  (see also ref. 6).

### Qualitative Predictions of Saturated Disk Model

Before discussing results of numerical modeling of diffusion plus the scheme in Eq. 2, we describe some qualitative features and inequalities. Following the terminology of Land *et al.* (1, 2), we define three quantities,  $a_q$ ,  $2t_d$ , and  $t_b$ . The post-synaptic quantal area ( $a_q = N/\sigma$ ) is that area containing a number of AcCho binding sites equal to the number of AcCho molecules in the released quantal packet ( $N$ ). The time  $2t_d = (0.8/4\pi) \times (N/\sigma D)$  [equation 3 of Land *et al.* (2)] is the characteristic time for released AcCho to diffuse over area  $a_q$  without binding;  $t_b = 0.93 h/(\sigma k_+)$  [equation 4 in Land *et al.* (2)] is the characteristic time for a single AcCho molecule to bind in the presence of excess receptor ( $h$  is the width of the cleft). By "saturating conditions" we mean that

( $\sigma/h$ ), the AcCho concentration that a quantal packet would have in the cleft over area  $a_q$ , is large compared with the dissociation constant  $K_d (= k_-/k_+)$ . If, in addition to saturating conditions, we also had  $t_b < 2t_d$ , then we would obtain a "saturated disk" of area  $a_q$  (where most receptor-channel complexes will be doubly bound) surrounded by a rim  $a_r$  of partially bound complexes. Because of excess receptors in the rim, the time that an AcCho molecule is free to diffuse is  $t_b$ , and the area of the rim  $a_r \approx (t_b) \times (D)$ . From the definition of  $t_d \approx a_q/2D$  we have

$$a_r/a_q \approx t_b/2t_d. \quad [4]$$

Unlike the rising phase (10, 11), the events associated with the falling phase of the MEPC should depend strongly on the presence of esterases. In the case in which all esterases are intact, no (or little) repeated binding is expected (17). The MEPC will then decay exponentially as  $e^{-(x-t)}$ . Thus  $\chi_-$  (the "apparent unbinding rate" in Eq. 2) is the inverse of the fall time with esterases intact. In the absence of esterases, the AcCho molecules released from receptors diffuse for a time of order  $t_b$  until they rebind to receptors, where they again stay a time  $1/\chi_-$  or the "apparent unbinding time." The only net change after such an AcCho "hopping cycle" in this process of "buffered diffusion" (12) is that the bound AcCho molecules are spread over an area larger by the rim  $a_r$  (Eq. 4). After  $H$  successive "hops," the quantal packet has spread over an area of about  $a_q + (H)(a_r)$ . When  $(H)a_r = a_q$ , the AcCho will have spread over an area  $2a_q$  and the MEPC amplitude will have fallen to half its peak value (due mainly to the number of AcCho molecules ineffective on singly ligated  $R_s$ ). The fall time in the absence of esterases is therefore the duration of one hopping cycle [given by the fall time with esterases intact ( $1/\chi_-$ ) multiplied by the number of hops ( $H$ ) needed to reach  $2a_q$  (i.e., when  $H = a_q/a_r = 2t_d/t_b$  from Eq. 4). Therefore, in the absence of esterases:

$$t_f \approx \frac{2t_d}{t_b} \times \frac{1}{\chi_-} \approx \frac{0.069}{h} \times \frac{gNk_+}{gD} \times \frac{1}{\chi_-}. \quad [5]$$

Thus the falling phase, with and without esterases, provides a means of deriving  $k_+/D$  distinct from that previously obtained from the rising phases (2).

Since  $t_f \propto N$  (Eq. 5) and since  $A_c$  increases with  $N$  [equation 2 of Land *et al.* (2)], the model predicts that when esterases are inactive there should be a positive correlation between  $t_f$  and  $A_c$ . Since there is a natural variation in  $N$  among quantal packets, such a correlation can be seen in our experiments (Fig. 2B).

According to Eq. 5,  $t_f$  should be independent of  $\sigma$ , but we must now introduce a correction that becomes appreciable when  $\sigma$  is small, namely, the loss of AcCho due to exit from the primary cleft (see also ref. 12). We model this loss by stipulating that any free AcCho disappears from the cleft when it has penetrated a radial distance  $R_{ex}$  from the source, and we consider  $R_{ex}$  as an adjustable parameter. We shall see that the area  $\pi R_{ex}^2$  is much larger than  $a_q = N/\sigma$  for the  $\sigma$  in the intact neuromuscular junction [15,000 sites per  $\mu m^2$  (2)]. However, when  $\sigma$  is decreased appreciably with BTX treatment, and especially for large  $N$ ,  $a_q$  approaches  $\pi R_{ex}^2$ . In that case the loss of AcCho from the cleft causes  $t_f$  to decrease. The extent of this effect under our experimental conditions is illustrated by the three theoretical curves corresponding to different values of  $R_{ex}$  in Fig. 2B and C: in Fig. 2B varying  $R_{ex}$  has relatively less effect on the curves than in Fig. 2C, where the curve is depressed radically for large  $A_c$  and small  $R_{ex}$ .

#### Fitting the Model Parameters

In ref. 2 we analyzed the data for the rising phase without including any back reactions (replacing the unbinding con-

stants  $k_-$  and  $\chi_-$  in Eq. 2 by zero). From the measured *mean* reduced rise time and mean amplitude (and the measured  $\sigma$  for the intact neuromuscular junction) we found one relationship between  $k_+$  and  $gD$ . In the present study we can derive an accurate value for  $\chi_-$  and a range of values for  $k_-$  from  $t_f$ , thus allowing us to include a consideration of the back reactions.

As suggested above, if esterases are fully efficient,  $\chi_- = 1/t_f$ . Since the esterases cannot be 100% efficient in preventing AcCho hopping, our experimental value for  $t_f = 1.16$  ms (Table 1) gives a lower limit to  $\chi_-$ , so that  $\chi_- \geq 0.86$  ms<sup>-1</sup>. Yet experimentally we see no evidence for hopping: if hopping were important, there would be a positive correlation between  $t_f$  and  $A_c$ . None is seen in Fig. 2A. Similarly, Anderson and Stevens (17) see no discrepancy in values for channel closing and current fall time when esterases are intact. We estimate measurement errors in these two experiments of at most about 30%. We thus carry out model fittings for values of  $\chi_-$  of both the lower limit of  $0.86$  ms<sup>-1</sup> and an upper limit of  $1.3 \times 0.86$  ms<sup>-1</sup>. With  $\chi_-$  fixed, we modeled MEPC shapes for the kinetic scheme in Eq. 2 plus AcCho diffusion for many choices of  $gD$ ,  $k_+$ ,  $k_-$ , and  $gN$ . The main results for each computation are values for  $A_c$ ,  $t_f$ , and  $t_r$ .

With  $\chi_-$  fixed, the parameters  $g$  and  $k_-$  are related uniquely by Eq. 3. If we assume a value for either  $g$  or  $k_-$ , model fitting to the experimentally obtained values for  $A_c$  and  $t_f$  from the present study and  $t_r$  from ref. 2 will give  $k_+$ ,  $D$ , and  $N$ . At present we can establish only a range for  $g$  (and  $k_-$ ) on the basis of the following two arguments: (i) Each computer calculation gives, in addition to values for  $A_c$ ,  $t_f$ , and  $t_r$ , the shape of the MEPC falling phase. For normal  $\sigma$  this shape depended somewhat on  $1 - g$  as illustrated in Fig. 3. The

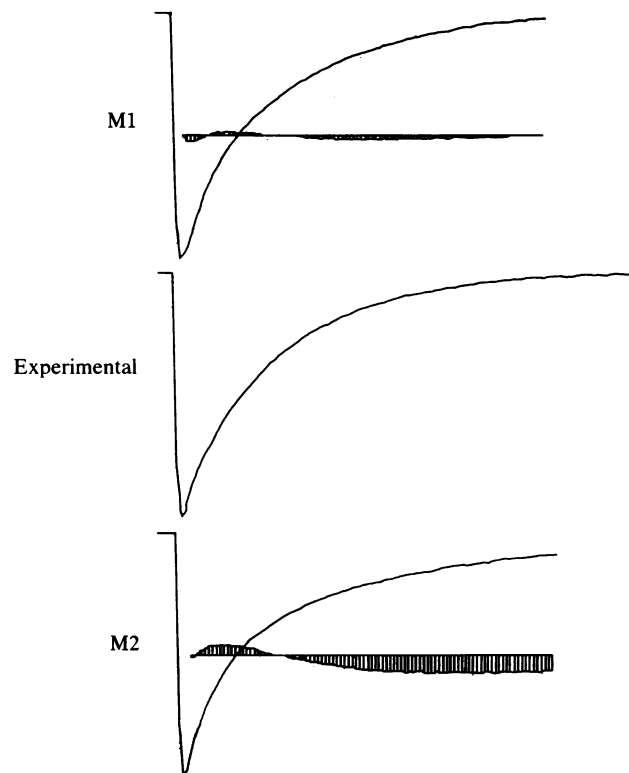


FIG. 3. Model and experimental MEPC waveforms. The trace labeled Experimental is the average of all MEPCs recorded in iPr<sub>2</sub>P-F (at this time scale the rising phase carries no information). The two model traces M1 and M2 are for  $(1 - g) = \chi_-/2k_- = 0.2$  (M1) or  $0.5$  (M2). Shaded curves are experimental minus model MEPCs. The fit is good for model M1 and generally for  $(1 - g) \leq 0.2$  (3% rms error). The relatively poor fit (16% rms error) in model M2 gets progressively worse for  $(1 - g) > 0.5$ .

predicted and observed MEPC falling phase are in reasonable agreement only if  $(1 - g) < 0.5$ . (ii) If we assume an upper limit of  $\approx 50 \mu\text{M}$  for  $K_d = k_-/k_+$  as often suggested (6, 16, 18–23), our previously derived value for  $k_+$  (2) gives  $k_- < 5 \text{ ms}^{-1}$  and thus  $(1 - g) > 0.1$ . We therefore adopt a value for  $1 - g$  between 0.1 and 0.5 and for  $k_-$  between 0.7 and  $5 \text{ ms}^{-1}$ . Possibilities of larger values for  $K_d$  and  $k_-$  will be analyzed in a later paper (see also Table 2).

For several values of  $k_-$  within the above range and for each of many assumed values of  $k_+/gD$  we carried out model calculations solving a coupled set of differential equations for diffusion and binding similar to Wathey *et al.* (24). Model fitting to observed  $A_c$  gives  $gN$ , and to the observed rise time (taken from ref. 2) gives  $gD$  and  $k_+$  through the following empirical relation:

$$0.62(3.27/k_+) + 0.36(3.9/gD) = 1 \pm 0.15 \quad [6]$$

with  $k_+$  in units of  $10^7 \text{ M}^{-1} \text{ s}^{-1}$  and  $D$  of  $10^{-6} \text{ cm}^2 \text{ s}^{-1}$ . To obtain  $k_+$  and  $gD$  from Eq. 6 uniquely, we still need the ratio  $k_+/gD$ , which is related to the ratio of  $t_f$  without and with esterases (see Eq. 5) and is obtained from the model fitting to the experimental  $t_f$ . Finally, we found that the computed relation between  $t_f$  and  $k_+/gD$  has a weak dependence on the assumed value for  $R_{ex}$  when  $\sigma$  is normal (Fig. 2B) and a strong dependence when  $\sigma$  is reduced by BTX treatment (Fig. 2C). Fitting the computations to the measured  $t_f$  for both experimental conditions (by a rapidly converging iteration process) thus refines  $k_+/gD$  and gives  $R_{ex}$ . Results are given in Table 2.

#### Observational Checks for Model Parameters

We had determined all the parameters in Table 2 (with an assumption of  $k_{-1} = k_{-2}$  and  $k_{+1} = k_{+2}$ ) using only the *mean* values for  $t_r$  and  $t_f$  but not their  $A_c$  dependency. We now have a number of observational checks: (i) in paper 2 the  $t_r$ – $A_c$  correlation gave a logarithmic slope  $\beta = 0.5 \pm 0.25$ . As explained in that paper, the theoretical value of  $\beta$  depends on the ratio  $k_+/gD$ . In the present paper we made an independent determination of  $k_+/gD$  entirely from the falling phase, and from this we calculated a value of  $\beta \approx 0.30$ , which is within our previously observed range of  $\beta$ . (ii) Similarly, the kinetic parameters give a calculated slope for the  $t_f$ – $A_c$  relation that fits the experimental results (Fig. 2B and C). (iii)

Table 2. Kinetic parameters

$k_{+1} = k_{+2} \equiv k_+ = (3.3 \pm 0.7) \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$
$\chi_- = 0.86 (+0.25, -0.05) \text{ ms}^{-1}$
$1 - g = \chi_-/2k_- = 0.1-0.5$
$k_{-1} = k_{-2} \equiv k_- = (0.7-5.5) \text{ ms}^{-1}$
$l_+ = (g) \times (25 \pm 10) \text{ ms}^{-1}$
$l_- = (1 - g) \times (25 \pm 10) \text{ ms}^{-1}$
$gD^* = (2.7 \pm 0.8) \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$
$gN^* = 6800 \pm 1400$
$R_{ex} = 1.6 \pm 0.3 \mu\text{m}$

Stated error ranges are estimated standard errors obtained from the square root of sum of squares of individual experimental errors. Final accuracy in  $l_+$ ,  $l_-$ ,  $D$ , and  $N$  is further limited by uncertainty in  $g$  ( $\approx 0.5-0.9$ ). Furthermore, if either  $gD$  or  $k_+$  is given, then Eq. 6 gives the other parameter more accurately than given in this table. \*To calculate  $N$  and  $D$  we need a value for single-channel conductance  $\gamma$  (see equations 2 and 3 of ref. 2). In this paper we used  $\gamma = 55 \text{ pS}$ , the value given by Hoffmann and Dionne (25) for the temperature used in the present study ( $22^\circ\text{C}$ ), but for snake endplates. If  $\gamma$  for the lizard should turn out to be different, the values of  $D$  and  $N$  in this table should both be multiplied by  $(55 \text{ pS}/\gamma)$ . If one should accept larger values of  $K_d$  and  $k_-$  or  $[(1 - g) < 0.1]$  then the value for  $k_+$  would be multiplied by the correction factor  $(l_+ + k_-)/l_+$  (26).

Because of the “receptor hopping,” one might expect the MEPC amplitude to decrease as  $t^{-1}$  for large time  $t$ . Yet for our adopted values of  $R_{ex}$  and  $1 - g$ , the calculated shape of the falling phase is almost exponential, as is the experimental shape (see Fig. 3).

## DISCUSSION

**Kinetic Parameters.** The main results of our present series of papers are the numerical values for nine parameters in Table 2: the six chemical kinetics parameters for the scheme in Eq. 1, the diffusion constant  $D$ , the distance  $R_{ex}$  to the exit from the cleft, and the mean number  $N$  of AcCho molecules per quantal packet. The equality of  $k_{+1}$  and  $k_{+2}$  in Table 2 is an assumption. The consequences of other values of the ratio  $k_{+1}/k_{+2}$  will be discussed in a later paper. We expect that postulating a much larger value of either  $k_{+1}$  or  $k_{+2}$  [which may be the case for carbamoylcholine (27)] will change the other parameters in Table 2 by factors of at most 2.

Even though we assume  $k_{-1} = k_{-2}$ , there is an apparent cooperativity in unbinding—unbinding from  $A_2R_c$  appears slower than from  $AR_c$ , because unbinding can occur only from the closed state. Thus the fraction of doubly bound closed channels,  $1 - g = 0.1-0.5$ , can be thought of as the “factor of effective cooperativity.” The effective dissociation constant  $\chi_-/k_+$  is then lower than  $k_-/2k_+$  by the same factor.

In paper 2 we omitted back reactions and derived values for the parameters  $k_+$ ,  $gD$ , and  $gN$  from the rising phase alone. In the present study we include back reactions and the falling phase. The ratio of fall times with and without esterases gives us an independent value for the ratio  $k_+/gD$  that is gratifyingly close to that obtained in paper 2. Furthermore, although the parameters  $k_-$  and  $(1 - g)$  are uncertain, the effective unbinding rate  $\chi_-$  is known quite accurately. Thus the model fitting (being relatively insensitive to  $k_-$ ) gives values for  $k_+$ ,  $gD$ , and  $gN$  with improved accuracy compared with those in paper 2 but within the previously derived ranges.

The diffusion rate constant is somewhat smaller than that for free diffusion [given as  $6-10 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$  (28–30)]. The value for  $N$  fits well with the experimentally derived upper limit of 10,000 from Kuffler and Yoshikami (31).

**Escape Route from Cleft.** Finally, a value of importance in determining the shape of the MEPC falling phase is  $R_{ex}$ , the typical distance from release site to edge of the cleft. Model fitting gave  $R_{ex}$  to be  $1.6 \mu\text{m}$ . To test this morphologically we measured the length of the primary cleft from 65 axonal end boutons, obtained from nine different animals. The average *half-length* of the primary cleft was  $2.6 \mu\text{m}$ , and the distance down the folds containing significant receptor is  $\approx 0.25 \mu\text{m}$  (8, 32). It is gratifying that our model value for  $R_{ex}$  falls between these two limits.

**Predictions for Single-Channel Recordings.** Since  $l_+$  is larger than  $2k_-$  (Table 2), we predict that the single channels total open time of about 1.2 ms (at  $22^\circ\text{C}$ ) will be interrupted by several brief closing gaps or “flickers,” during which no unbinding of AcCho would occur. The mean number of such closings should be  $l_+/2k_- \approx 1.5-10$ , the mean duration of each individual “closed-state spike” would be only  $l_+^{-1} \approx 60 \mu\text{s}$ , and each “open spike”  $l_-^{-1} \approx 50-600 \mu\text{s}$ . Several studies (e.g., refs. 3 and 33), but not all (ref. 4), show such multiple closings, thus verifying qualitatively our assertion that isomerization is more rapid than unbinding.

**Buffered Diffusion.** The pioneering paper by Katz and Miledi (ref. 12; see also ref. 15) developed the concept of “buffered diffusion” for the falling phase of a MEPC in the absence of esterases. They defined a ratio  $(1 - p)/p$  of unbound to bound molecules. In our notation this equals the ratio of  $t_b$ , the time molecules are free to diffuse (2), to  $1/\chi_-$ ,

the time to unbind. From data on the rising phase (2) we now have direct estimates for  $t_b$  and thereby calculate  $p$  to be  $\approx 0.95$  for normal  $\sigma$  and 0.85 after BTX treatment. Katz and Miledi had to assume much smaller values of  $p$  than our measured values to account for the large drop in MEPC amplitude when  $\sigma$  is decreased. However, this is no longer needed, since evidence is now strong that 2 AcCho molecules are required to open a channel (e.g., refs. 1, 10, 16, and 34–36). This can account for the drop in amplitude due to wastage of AcCho on partially blocked receptor complexes (1, 10, 11, 27).

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